

Input testing: Partition and combinatorial testing

Angelo Gargantini –
Corso Testing e verifica del software

Outline

- ▶ Input testing
- ▶ Partition testing
 - ▶ A method to apply partition testing
 - ▶ How to choose variable values
- ▶ Combinatorial interaction of parameters
 - What is combinatorial testing
 - **Efficiency:** It can detect faults
- ▶ Generation techniques
 - ▶ IPO, AETG, IPOS
- ▶ Adding constraints
 - ▶ Logic approach, using SAT/SMT solving

What is Input testing

- ▶ “input space” testing or testing based on the **interfaces**
- ▶ No internal information about the system under test is considered, but only the information about the inputs
- ▶ It can be model based testing
 - ▶ Model of the inputs
- ▶ Program based testing
 - ▶ The program is analyzed to extract the parameters
 - ▶ E.g. the parameters of a method. ...

Advantages of Input based testing

- ▶ Can be equally applied at several levels of testing
 - ▶ Unit
 - ▶ Integration
 - ▶ System
- ▶ Relatively easy to apply
 - ▶ Test generation is simple, simpler than structure based testing or fault based
- ▶ Easy to adjust the procedure to get more or fewer tests
- ▶ No implementation knowledge is needed
 - ▶ just the input space
 - ▶ Usable even if the complete code/model is not accessible

Partition testing

Problems ...

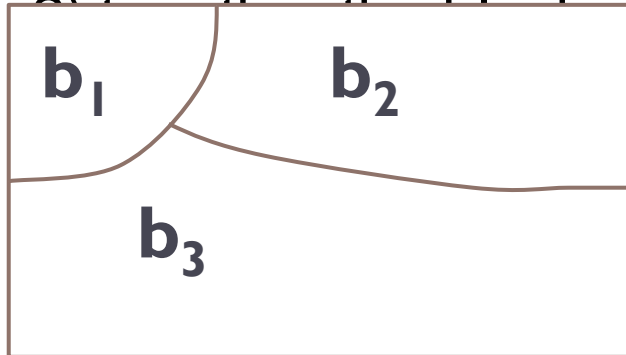
- ▶ The input domain to a program contains all the possible inputs to that program
 - ▶ For even small programs, the input domain is so large that it might as well be infinite
- ▶ Testing is fundamentally about choosing finite sets of values from the input domain

Solution: Input partitioning

- ▶ Domain for each input parameter is partitioned into regions
 - ▶ The domain is substituted by an enumeration

Partitioning Domains

- ▶ Domain D
- ▶ Partition scheme q of D
- ▶ The partition q defines a set of blocks, $Bq = b_1, b_2, \dots, b_Q$
- The partition must satisfy two properties:
 - 1) blocks must be pairwise disjoint (no overlap)



2) the blocks must cover the domain D (no holes)

$$b_i \cap b_j = \Phi, \forall i \neq j, b_i, b_j \in Bq$$

$$\bigcup_{b \in Bq} b = D$$

Using Partitions – Assumptions

- ▶ Choose a value from each partition
- ▶ Each value is assumed to be equally useful for testing
- ▶ Application to testing
 - ▶ Find characteristics in the inputs : parameters, semantic descriptions, ...
 - ▶ Partition each characteristics
 - ▶ Choose tests by combining values from characteristics
- ▶ Example Characteristics
 - ▶ Input X is null -> true or false
 - ▶ Order of the input file F -> sorted, inverse sorted, arbitrary
 - ▶ Min separation of two aircraft -> integer 0 ... 1000
 - ▶ Input device -> DVD, CD, VCR, computer

Choosing Partitions

- ▶ Choosing (or defining) partitions seems easy, but is easy to get wrong
- ▶ Consider a file the contains word in some “order”

b1 = sorted in ascending order
b2 = sorted in descending order
b3 = arbitrary order

Solution:

Each characteristic should address just one property
b1 and b2

but ... something's fishy ...

What if the file is of length 1?

**The file will be in all three blocks ...
That is, disjointness is not satisfied**

File F sorted ascending

- b1 = true
- b2 = false

File F sorted descending

- b1 = true
- b2 = false

Properties of Partitions

- ▶ If the partitions are not complete or disjoint, that means the partitions have not been considered carefully enough
- ▶ They should be reviewed carefully, like any design attempt
- ▶ Different alternatives should be considered

Example for program based testing

- ▶ Java

```
enum Color { RED, GREEN, BLU}  
  
void foo(long x, Color c, boolean value)
```

Color and boolean domain already partitioned. What about long domain?

Example of partition, from **Boundary Value Analysis**

- ▶ **MAX_VALUE**

A constant holding the maximum value a long can have, $2^{63}-1$.

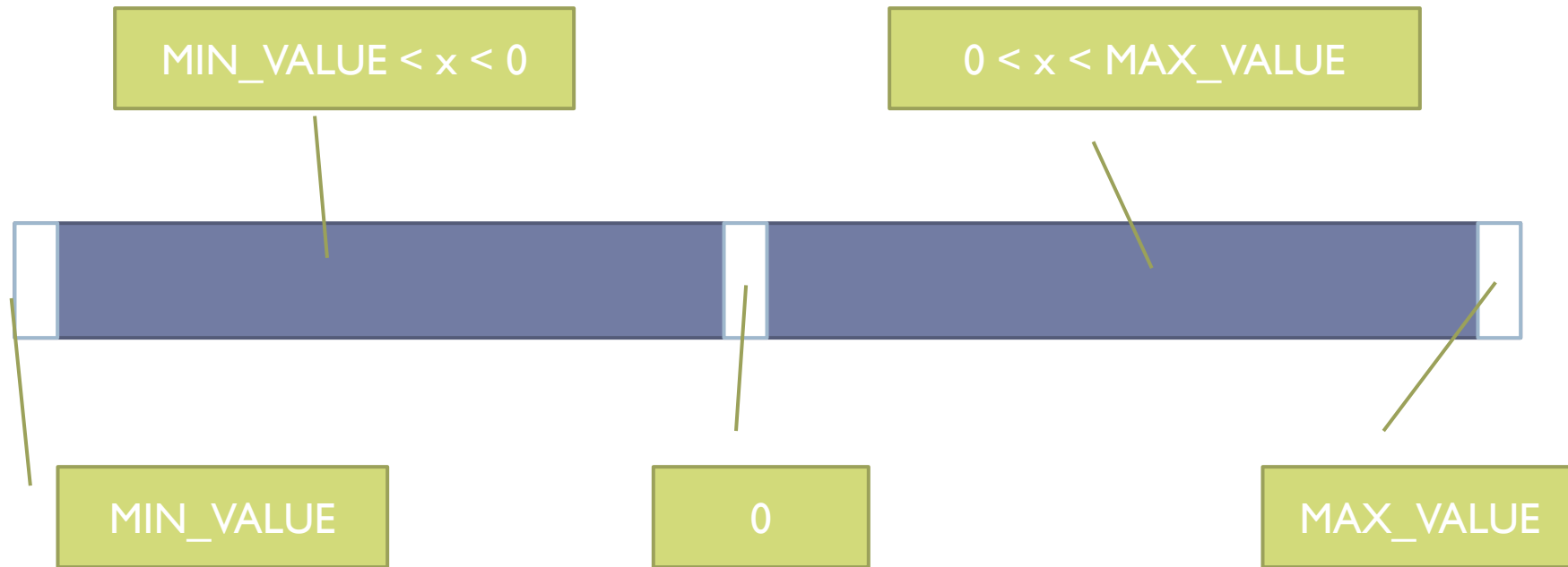
- ▶ **MIN_VALUE**

A constant holding the minimum value a long can have, -263.

- ▶ **BETWEEN MAX E MIN?**

Partition for long

Partitions in 5 subsets



What to do when a Domain is a product of domains

- ▶ When our domain $D = D1 \times D2 \times D3 \dots$
- ▶ example: `foo(int x, enum y, string s)`
 $D = \text{int} \times \text{enum} \times \text{string}$
- ▶ Three possible choices:
 - Partition D as a whole
 - Partition D_i and make the cartesian product
 - Partition D_i and apply combinatorial testing

Partition of cartesian product

- ▶ Given two domains D1 and D2
- ▶ Let P1 a partition for D1 and P2 a partition for D2
- ▶ Partitions can be multiplied to obtain again partitions
- ▶ $D1 \times D2$ can be partitioned by $P1 \times P2$

- ▶ $P1 \times P2$ will contain all the combinations of P1 and P2

| | | | | |
|----|-----|-----------|-----|-----|
| D1 | d11 | (d11,d21) | .. | .. |
| | d12 | ... | .. | .. |
| | d13 | ... | .. | .. |
| | | d21 | d22 | d23 |
| | | D2 | | |

Product of partitions, application

- ▶ For more than one input:

```
/** given three sides return the type  
    of the triangle*/
```

```
TriType Triang(int Side1,int Side2,int Side3)
```

- ▶ If one splits every input in 5 subsets, the input is partitioned in $5 \times 5 \times 5 = 125$ subsets
-

Partition testing

- ▶ Several methods are based on partition testing [see books by Myers, and Beizer]:
 1. Equivalent Partition
 2. Domain Testing
 3. Boundary Value Analysis
 4. Category Partition [Ostrand Balcer 1988]:
 - ▶ Identify the parameters and variables and their choices
 - ▶ Generate all combinations (test frames)
-

Partition does not solve the problem!

- ▶ Category partition testing gave us
 - ▶ Systematic approach: Identify characteristics and values (the creative step),
 - ▶ generate combinations (the mechanical step)
 - ▶ While equivalence partitioning offers a set of guidelines to design test cases, it suffers from two shortcomings:
 1. It raises the possibility of a large number of sub-domains in the partition.
 - ▶ Test suite size grows very rapidly with number of categories. Can we use a non-exhaustive approach?
 2. It lacks guidelines on how to select inputs from various sub-domains in the partition.
-

INPUT DOMAIN MODELLING

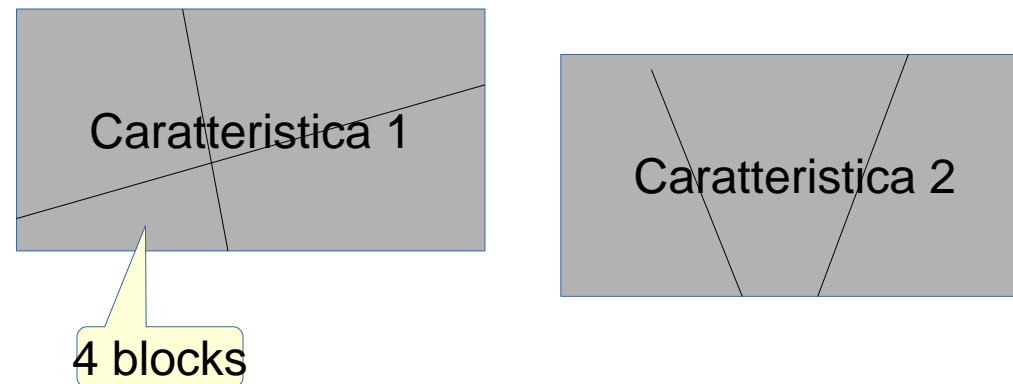
How to select the inputs and their values

A. Input Domain Modeling

- ▶ **Step 1 : Identify testable functions**
 - ▶ Individual methods have one testable function
 - ▶ In a class, each method has the same characteristics
 - ▶ Programs have more complicated characteristics—modeling documents such as UML use cases can be used to design characteristics
 - ▶ Systems of integrated hardware and software components can use devices, operating systems, hardware platforms, browsers, etc
 - **Step 2 : Find all the parameters**
 - Often fairly straightforward, even mechanical
 - Important to be complete
 - Methods : Parameters and state (non-local) variables used
 - Components : Parameters to methods and state variables
 - System : All inputs, including files and databases
-

Modeling the Input Domain (cont)

- ▶ **Step 3 : Model the input domain**
 - ▶ The domain is scoped by the parameters
 - ▶ The structure is defined in terms of characteristics
 - ▶ Each characteristic is partitioned into sets of blocks
 - ▶ Each block represents a set of values
 - ▶ This is the most creative design step in applying ISP



STEP 3: Modeling the Input Domain

- ▶ Partitioning characteristics into blocks and values is a very creative engineering step
- ▶ More blocks means more tests
- ▶ The partitioning often flows directly from the definition of characteristics and both steps are sometimes done together
 - ▶ Should evaluate them separately – sometimes fewer characteristics can be used with more blocks and vice versa
- ▶ Strategies for identifying values :
 - ▶ Include valid, invalid and special values
 - ▶ Sub-partition some blocks
 - ▶ Explore boundaries of domains
 - ▶ Include values that represent “normal use”
 - ▶ Try to balance the number of blocks in each characteristic
 - ▶ Check for completeness and disjointness

Two Approaches to Input Domain Modeling (IDM)

I. Interface-based approach

- ▶ Develops characteristics directly from individual input parameters
- ▶ Simplest application
- ▶ Can be partially automated in some situations

I. Functionality-based approach

- ▶ Develops characteristics from a behavioral view of the program under test
- ▶ Harder to develop—requires more design effort
- ▶ May result in better tests, or fewer tests that are as effective

1. Interface-Based Approach

- ▶ Mechanically consider each parameter in isolation
- ▶ This is an easy modeling technique and relies mostly on syntax
- ▶ Some domain and semantic information won't be used
 - ▶ Could lead to an incomplete IDM
- ▶ Ignores relationships among parameters

Consider TriTyp

Three *int* parameters

IDM for each parameter is identical

Reasonable characteristic : *Relation of side with zero*

2. Functionality-Based Approach

- ▶ Identify characteristics that correspond to the intended functionality
- ▶ Requires more design effort from tester
- ▶ Can incorporate domain and semantic knowledge
- ▶ Can use relationships among parameters
- ▶ Modeling can be based on requirements, not implementation
- ▶ The same parameter may appear in multiple characteristics, so it's harder to translate values to test cases

Consider TriTyp again

The three parameters represent a *triangle*

IDM can combine all parameters

Reasonable characteristic : *Type of triangle*

Interface-Based IDM – TriTyp

- TriTyp, had one testable function and three integer inputs

First Characterization of TriTyp's Inputs

| Characteristic | b_1 | b_2 | b_3 |
|-----------------------------------|----------------|------------|-------------|
| q_1 = "Relation of Side 1 to 0" | greater than 0 | equal to 0 | less than 0 |
| q_2 = "Relation of Side 2 to 0" | greater than 0 | equal to 0 | less than 0 |
| q_3 = "Relation of Side 3 to 0" | greater than 0 | equal to 0 | less than 0 |

- ▶ A maximum of $3*3*3 = 27$ tests
- ▶ Some triangles are valid, some are invalid
- ▶ Refining the characterization can lead to more tests ...

Second Characterization of TriTyp's Inputs

| Characteristic | b_1 | b_2 | b_3 | b_4 |
|---|----------------|------------|------------|-------------|
| $q_1 = \text{"Refinement of } q_1 \text{"}$ | greater than 1 | equal to 1 | equal to 0 | less than 0 |
| $q_2 = \text{"Refinement of } q_2 \text{"}$ | greater than 1 | equal to 1 | equal to 0 | less than 0 |
| $q_3 = \text{"Refinement of } q_3 \text{"}$ | greater than 1 | equal to 1 | equal to 0 | less than 0 |

- ▶ A maximum of $4 \times 4 \times 4 = 64$ tests
- ▶ This is only complete because the inputs are integers (0 .. 1)

Possible values for partition q_1

| Characteristic | b_1 | b_2 | b_3 | b_4 |
|----------------|-------|-------|-------|-------|
| Side1 | 2 | 1 | 0 | -1 |

Testing e verifica del SW 22/23

Test boundary conditions

Functionality-Based IDM – TriTyp

- ▶ First two characterizations are based on syntax–parameters and their type
- ▶ A semantic level characterization could use the fact that the three integers represent a triangle

Geometric Characterization of TriTyp's Inputs

| Characteristic | b_1 | b_2 | b_3 | b_4 |
|---|---------|-----------|-------------|---------|
| $q_1 = \text{"Geometric Classification"}$ | scalene | isosceles | equilateral | invalid |

- Oops ... something's fishy ... equilateral is also isosceles !
- We need to refine the example to make characteristics valid

Correct Geometric Characterization of TriTyp's Inputs

| Characteristic | b_1 | b_2 | b_3 | b_4 |
|---|---------|----------------------------|-------------|---------|
| $q_1 = \text{"Geometric Classification"}$ | scalene | isosceles, not equilateral | equilateral | invalid |

Testing e verifica del SW 22/23

At the end of the first 3 steps

- Set of parameters
 - Each parameter has a list of possible values
 - Each value represent a block
 - Each value can represent a partition
- There may be constraints over the possible values

Combination Strategies criteria

- ▶ Step 4 : Apply a test criterion to choose combinations of values
 - A test input has a value for each parameter
 - One block for each characteristic
 - Choosing all combinations is usually infeasible
 - Coverage criteria allow subsets to be chosen
- ▶ Step 5 : Refine combinations of blocks into test inputs
 - Choose appropriate values from each block

Choosing Combinations of Values

- We assume to have partitioned the domain in characteristics and partitioned each characteristic in blocks



Step 4 – Choosing Combinations of Values

- ▶ Once characteristics and partitions are defined, the next step is to choose test values
 - We use criteria – to choose effective subsets
- ▶ The most obvious criterion is to choose all combinations ...

All Combinations (ACoC) : All combinations of blocks from all characteristics must be used.

- Number of tests is the product of the number of blocks in each characteristic :

$$\prod_{i=1}^Q B_i$$

- The second characterization of TriTyp results in $4*4*4 = \underline{64 \text{ tests}}$ – too many ?

Example

- Characteristic1: color : {Green, White, Red}
- Characteristic2: age [0...100] : blocks [0..6] [7..40][41..100]
- Characteristic3: isFemale : {true, false}
- ACoC all the combinations of blocks
 - (not the combinations of all the values)
- Combination I: Green, 5,true
- If every block has only a value is like taking all the combinations of values.

ISP Criteria – Each Choice

- ▶ 64 tests for TriTyp is almost certainly way too many
- ▶ One criterion comes from the idea that we should try at least one value from each block

Each Choice (EC) : One value from each block for each characteristic must be used in at least one test case.

- Number of tests is the number of blocks in the largest characteristic

$$\max_{i=1}^Q \text{size}(B_i)$$

For TriTyp

- ▶ Three inputs side1, side2, side3
- ▶ Four values each 2, 1, 0, -1

- ▶ A test with 4 test is enough:

2, 2, 2

1, 1, 1

0, 0, 0

-1, -1, -1

Each Choice (EC)

- Characteristic1: color : {Green, White, Red}
- Characteristic2: age [0...100] : blocks [0..6] [7..40][41..100]
- Characteristic3: isFemale : {true, false}
- Each Choice (EC)
 - 3 Combination:
Green, 5,true
...
- Is there something in the middle?

- ▶ AoC “Too many” ! - EC too few



- ▶ 34 switches = $2^{34} = 1.7 \times 10^{10}$ possible inputs = 1.7×10^{10} tests ????

- ▶ Too much – some assumptions
 - What if we knew that **one** single switch always causes the fault?
2 tests would be enough to find if the system is correct:
 - all off, all onWhat if we knew no failure involves more than 2 **switch** settings interacting?
 - We should test the interaction of 2 switches

Tra eachchoice e allcombinations

▶ Esempio introduttivo a combinatorial

– Per comodità ogni blocco ha un valore

| CLIENT | WEB SERVER | PAYMENT | DATABASE |
|---------|------------|-------------|----------|
| FIREFOX | WEB SPHERE | MASTER CARD | DB/2 |
| IE | APACHE | VISA | ORACLE |
| OPERA | .NET | | |

- All combinations...
- Each choice

- Se volessi testare tutti a coppia- coppia
 - Per vedere se l'interazione tra due può dare errore
 - Esempio FIREFOX su WEBSHERE, ma anche FIRE



ISP Criteria – Pair-Wise

- Another approach asks values to be combined with other values

Pair-Wise (PW) :A value from each block for each characteristic must be combined with a value from every block for each other characteristic.

For TriTyp:

| | | | |
|------------------|-----------------|-----------------|------------------|
| 2, 2, 2 | 2, 1, 1 | 2, 0, 0 | 2, -1, -1 |
| 1, 2, 1 | 1, 1, 0 | 1, 0, -1 | 1, -1, 2 |
| 0, 2, 0 | 0, 1, -1 | 0, 0, 2 | 0, -1, 1 |
| -1, 2, -1 | -1, 1, 2 | -1, 0, 1 | -1, -1, 0 |

Example

- Characteristic1: color : {Green, White, Red}
- Characteristic2: age [0...100] : blocks [0..6] [7..40][41..100]
- Characteristic3: isFemale : {true, false}
- PW. chose two characteristics: every combination of values of these two characteristics is covered
- Color and age: every pair must be covered
- Age and isFemale must be covered
-

Combinatorial approach

- Pairwise combination instead of exhaustive
 - Generate combinations that efficiently cover all pairs of values
 - Rationale: most failures are triggered by single values or combinations of a few values. Covering pairs (triples,...) reduces the number of test cases, but reveals most faults

Example

| Display Mode | Color | Screen size |
|---------------------|--------------|--------------------|
| full-graphics | Monochrome | Hand-held |
| Low resolution | 16-bit | Laptop |
| text-only | True-color | Full-size |

- 3 variables with 3 values each: $3^3 = 27$ possible combinations
- Combinatorial testing with much fewer tests

Test Suite - example

- ▶ pairwise testing can be achieved by only 9 tests

| Test | Color | Display Mode | Screen Size |
|------|------------|---------------|-------------|
| 1 | Monochrome | Full-graphics | Hand-held |
| 2 | 16-bit | Text-only | Laptop |
| 3 | True-color | Full-graphics | Hand-held |
| 4 | ... | ... | ... |

One test covers many combinations:
e.g. Test 1 covers 3 pairs:
(Monochrome, Full-graphics)
(Monochrome, Hand-held)
(Full-graphics, Hand-held)

Other figures:

2^{100} combinations with 10 tests;
 10^{20} -> 200 tests; ...

ISP Criteria – Pair-Wise

- Number of tests?

- Number of tests is at least the product of two largest characteristics

$$\left(\text{Max}_{i=1}^Q |B_i| \right) * \left(\text{Max}_{j=1, j \neq i}^Q |B_j| \right)$$

ISP Criteria –T-Wise

- A natural extension is to require combinations of t values instead of 2

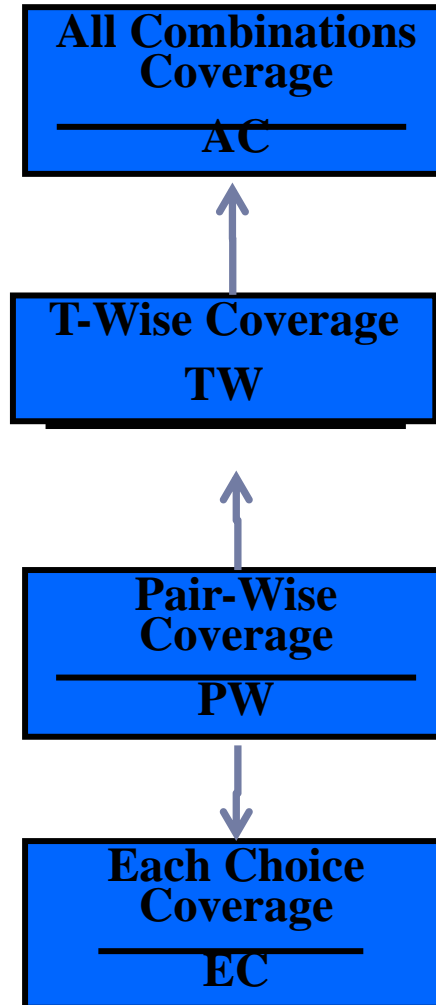
t-Wise (TW) :A value from each block for each group of t characteristics must be combined.

- Number of tests is at least the product of t largest characteristics
- If all characteristics are the same size, the formula is

$$\left(\text{Max}_{i=1}^Q \text{size}(B_i)\right)^t$$

- If t is the number of characteristics Q , then all combinations
- That is ... Q -wise = AC
- t -wise is expensive and benefits are not clear

ISP Coverage Criteria Subsumption



Exercise

- example system: component based application

| CLIENT | WEB SERVER | PAYMENT | DATABASE |
|---------|------------|-------------|----------|
| FIREFOX | WEB SPHERE | MASTER CARD | DB/2 |
| IE | APACHE | VISA | ORACLE |
| OPERA | .NET | AMEX | ACCESS |

One test is missing ...

- ▶
- ▶ ▶ $3^4 = 81$ exhaustive test cases
- ▶ 9 test cases

| CLIENT | WEB SERVER | PAYMENT | DATABASE |
|---------|------------|-------------|----------|
| FIREFOX | WEB SPHERE | MASTER CARD | DB/2 |
| FIREFOX | .NET | AMEX | ORACLE |
| FIREFOX | APACHE | VISA | ACCESS |
| IE | WEB SPHERE | AMEX | ACCESS |
| IE | APACHE | MASTER CARD | ORACLE |
| IE | .NET | VISA | DB/2 |
| OPERA | WEB SPHERE | VISA | ORACLE |
| OPERA | .NET | MASTER CARD | ACCESS |
| OPERA | APACHE | AMEX | DB/2 |

Altri criteri

- Esistono anche altri criteri come il
- **Base Choice Coverage (BCC):** A base choice block is chosen for each characteristic, and a base test is formed by using the base choice for each characteristic. Subsequent tests are chosen by holding all but one base choice constant and using each non-base choice in each other characteristic.
- BCC prevede un test (base) + una variazione per ogni blocco di ogni partizione
 - Esempio – triangolo base choice
 - -1,0,1,2 per ogni lato, e base 2,2,2 ...

Estensione

- Multiple base choice.
- Multiple Base Choices (MBCC): At least one, and possibly more, base choice blocks are chosen for each characteristic, and base tests are formed by using each base choice for each characteristic at least once. Subsequent tests are chosen by holding all but one base choice constant for each base test and using each non-base choice in each other characteristic.
- Più semplici da generare che i combinatorial test suite

A small simplification

- In case every characteristic is an input variable
- That takes the value in a domain and each block is a **single** value in this domain
- Example input I: {A,B,C}, input {LOW,MIDDLE,HIGH}
- Each choice: every possible combination of values is given to all the variables
- One choice: every variable takes at least once
- Pairwise: every pair of values is taken by at least one test



- Generation techniques per combinatorial testing

Generation techniques families

- Algebraic
 - Based on some mathematical/algebraic properties
- Search based, greedy, based on heuristics
 - Because the problem of generating a minimum test suit for combinatorial testing is NP-complete, most methods and tools use a greedy approach
- Logic based
 - Based on SAT/SMT solving and model checking

Classification

- Algebraic methods that are mainly developed by mathematicians
 - Latin squares, Orthogonal arrays, Covering arrays
 - Recursive Construction
- Search-Based methods that are mainly developed by computer scientists
 - AETG (from Telcordia), TCG (from JPL/NASA), DDA (from ASU), PairTest/Fireeye (from NIST)
 - Incremental construction

Search-Based vs Algebraic Methods

- Algebraic methods:
 - Advantages: very fast, and often produces optimal results
 - Disadvantages: limited applicability, difficult to support parameter relations and constraints
 - E.g. most work only if all the parameters have the same domain size
- Search-based methods:
 - Advantages: no restrictions on the input model, and very flexible, e.g., relatively easier to support parameter relations and constraints
 - Disadvantages: explicit search takes time, the resulting test sets are not optimal

Greedy methods

Greedy methods

- Parameter based
 - One column at the time
 - IPO
 - IPOS – still room to improve
- Test case based
 - Add one test at the time
 - AETG

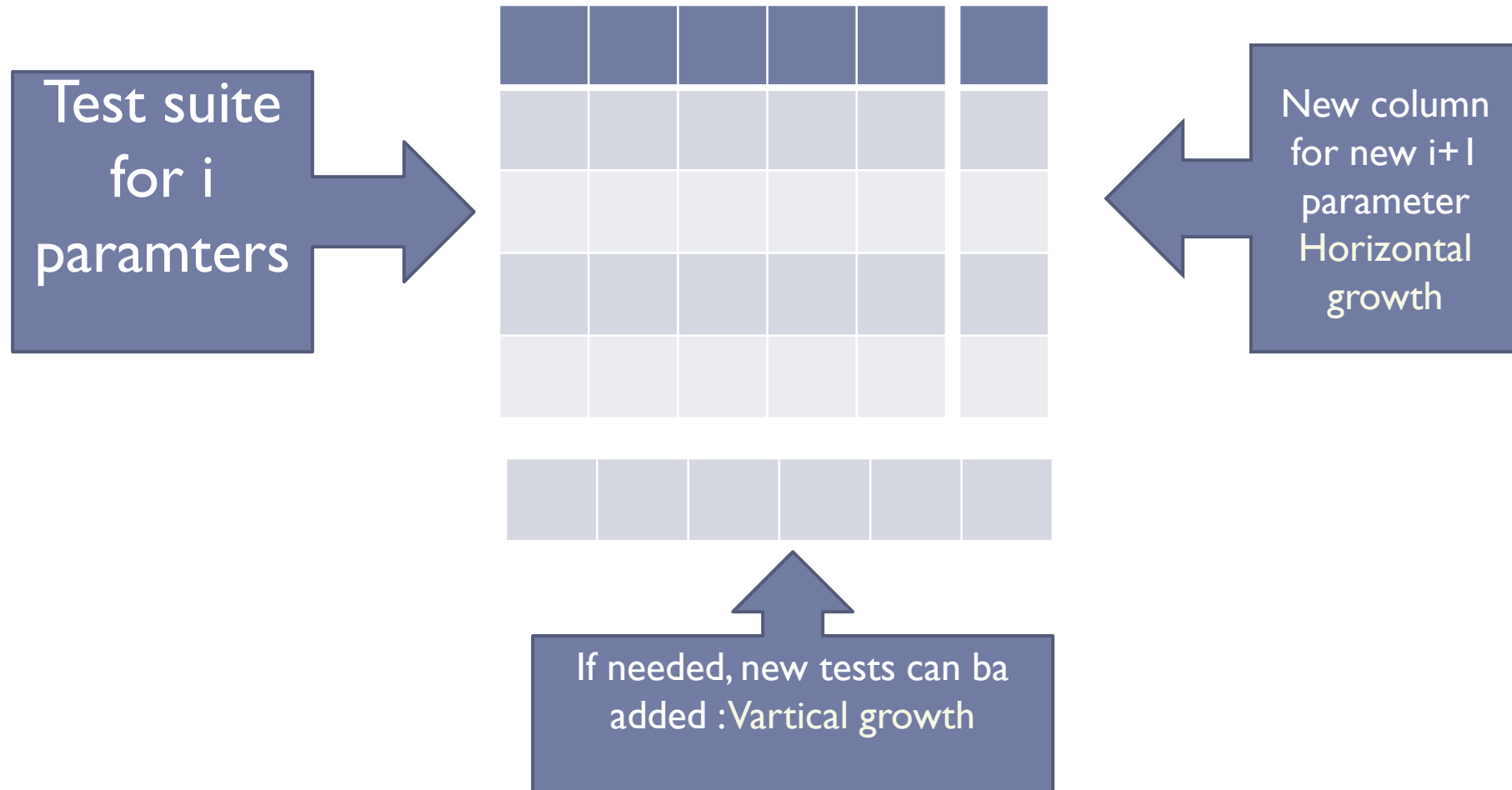
IPO: In-Parameter-Order

- Originally presented in:
- Yu Lei, K. C. Tai, "In-Parameter-Order: A Test Generation Strategy for Pairwise Testing," High-Assurance Systems Engineering, IEEE International Symposium on, p. 254, Third IEEE International High-Assurance Systems Engineering Symposium, 1998
- Several extensions
- NIST
- <http://csrc.nist.gov/groups/SNS/acts/>
- TOOL: FireEye, now ACTS

IPO: In-Parameter-Order

- Builds a t-way test set in an incremental manner
 - A t-way test set is first constructed for the first t parameters, simply considering their combinations
 - Then, the test set is extended to generate a t-way test set for the first t + 1 parameters
 - The test set is repeatedly extended for each additional parameter.
- Two steps involved in each extension for a new parameter:
 - Horizontal growth: extends each existing test by adding one value of the new parameter
 - Vertical growth: adds new tests, if necessary

Adding parameters



Strategy In-Parameter-Order

- /* step 1: for the first t parameters p1, p2 , ..., pt*/
- $T := \{(v1, v2, \dots, vt) \mid v1, v2, \dots, vt \text{ are values of } p1, p2, \dots, pt\}$ // cartesian product
- if $n = t$ then stop;
- /* step 2: for the remaining parameters */
- for parameter $p_i, i = t + 1, \dots, n$ do
- begin /* add parameter p_i */
- /* 2a: horizontal growth */
- for each test $(v1, v2, \dots, v_{i-1})$ in T do
- replace it with $(v1, v2, \dots, v_{i-1}, v_i)$, where v_i is a value of p_i
- /* 2b: vertical growth */
- while T does not cover all the interactions between p_i and
- each of $p1, p2, \dots, p_{i-1}$ do
- add a new test for $p1, p2, \dots, p_i$ to T;
- end

Example

- Consider a system with the following parameters and values:
 - parameter A has values WIN and LIN
 - parameter B has values INT and AMD, and
 - parameter C has values IPV4, IPV6

- Pairwise testing $t = 2$

Step 1: the first t parameters

- if a test suite wants to cover all the t-combinations of t parameters, it must contain all the possible combinations
- $t = 2$
- parameter A has values WIN and LIN
- parameter B has values 1NT and AMD
- Initial test suite (CA):

| A | B |
|-----|-----|
| WIN | INT |
| WIN | AMD |
| LIN | INT |
| LIN | AMD |

Step 2: adding a new parameter

- Add the tests to cover the $t+1$ th parameter.
- Add a column to the CA for the new parameter
- For the values of the new

Horizontal Growth

| A | B |
|-----|-----|
| WIN | INT |
| WIN | AMD |
| LIN | INT |
| LIN | AMD |

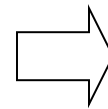


| A | B | C |
|-----|-----|------|
| WIN | INT | IPV4 |
| WIN | AMD | IPV6 |
| LIN | INT | IPV4 |
| LIN | AMD | IPV6 |

Step 2 b

- Check if all the tuples are covered, in case add new rows (vertical growth)

| A | B | C |
|-----|-----|------|
| WIN | INT | IPV4 |
| WIN | AMD | IPV6 |
| LIN | INT | IPV4 |
| LIN | AMD | IPV6 |



Vertical Growth

| A | B | C |
|-----|-----|------|
| WIN | INT | IPV4 |
| WIN | AMD | IPV6 |
| LIN | INT | IPV4 |
| LIN | AMD | IPV6 |
| LIN | AMD | IPV4 |
| LIN | INT | IPV6 |

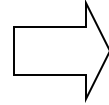
missing :
AMD, IPV4
INT, IPV6

Exercise

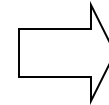
- parameter A has values A1 and A2
- parameter B has values B1 and B2, and
- parameter C has values C1, C2, and C3

Example (2)

| A | B |
|----|----|
| A1 | B1 |
| A1 | B2 |
| A2 | B1 |
| A2 | B2 |



| A | B | C |
|----|----|----|
| A1 | B1 | C1 |
| A1 | B2 | C2 |
| A2 | B1 | C3 |
| A2 | B2 | C1 |



| A | B | C |
|----|----|----|
| A1 | B1 | C1 |
| A1 | B2 | C2 |
| A2 | B1 | C3 |
| A2 | B2 | C1 |
| A2 | B1 | C2 |
| A1 | B2 | C3 |

Horizontal Growth

Vertical Growth

Open problems

- When adding a new column, how to choose the values?
- When adding a new row, how to choose the new row?

Combinatorial testing is effective

What is Combinatorial testing

- ▶ It can be classified “input space” testing or testing based on the **interfaces**
- ▶ Systematic testing of parameters to check the interaction

CIT effectiveness

- ▶ Experiments show that CIT is
- ▶ effective
 - ▶ finds faults that traditional testing may be not able to find
- ▶ efficient
 - ▶ A low degree of interaction between inputs can already discover most faults
 - ▶ Pairwise is the most used
 - ▶ Never with interaction > 6

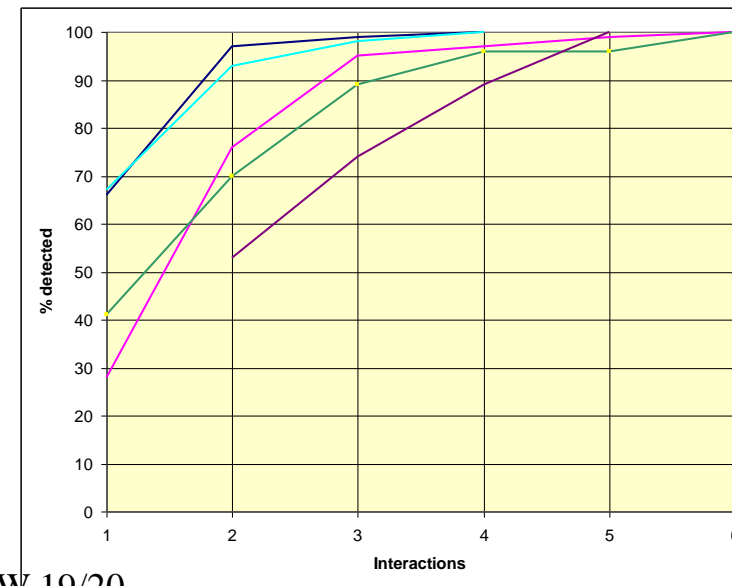
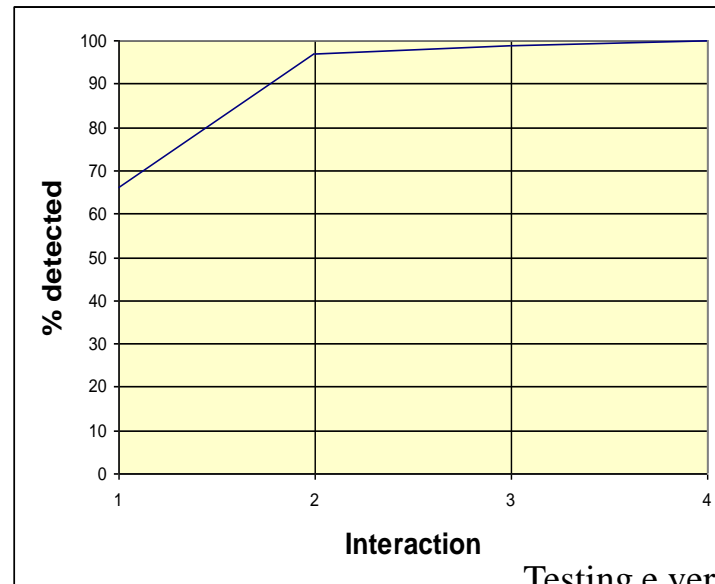
Effectiveness -1

- ▶ *Compared to a traditional company that would use the quasi-exhaustive strategy, the combinatorial design method (CDM) strategy would reduce its system level test schedule by sixty-eight percent (68%) and save sixty-seven percent (67%) in labor costs associated with the testing.*

- ▶ *Reference: Raytheon (2000). Jerry Huller. Reducing Time to Market with Combinatorial Design Method Testing.*

Effectiveness -2 - Kuhn @ NIST

- ▶ Maximum interactions for fault triggering was 6
- ▶ Reasonable evidence that maximum interaction strength for fault triggering is relatively small
 - ▶ % errors (seeded or found) vs interaction strength for several application:



Testing e verifica del SW 19/20

Testing e verifica del SW 22/23

Effectiveness - 3

- ▶ More experiments are needed
- ▶ New experiments are welcome!

*Combinatorial testing is better
than structural testing ?*

*Combinatorial testing is better
than random testing ?*

VINCOLI TRA I PARAMETRI

- Molte volte I parametri non sono indipendenti ma esistono dei vincoli
- Esempi
 - Giorno e mese
 - Se mese = FEB, giorno < 29

Vincoli

| CLIENT | SISTEMA OP. | ARCH |
|---------|-------------|-----------|
| FIREFOX | WINDOWS | X86-32bit |
| IE | LINUX | X86-64bit |
| OPERA | MACOS | ARM |

- Constraints:
 - CLIENT = IE => SISTEMAOP = WINDOWS
 - not (SO = MACOS and ARCH = ARM)
 -
 -