

# 1 Program verification

The methods of the previous chapter are suitable for verifying systems of communicating processes, where control is the main issue, but there are no complex data. We relied on the fact that those (abstracted) systems are in a finite state. These assumptions are not valid for sequential programs running on a single processor, the topic of this chapter. In those cases, the programs may manipulate non-trivial data and – once we admit variables of type integer, list, or tree – we are in the domain of machines with infinite state space. In terms of the classification of verification methods given at the beginning of the last chapter, the methods of this chapter are

**Proof-based.** We do not exhaustively check every state that the system can get in to, as one does with model checking; this would be impossible, given that program variables can have infinitely many interacting values. Instead, we construct a proof that the system satisfies the property at hand, using a proof calculus. This is analogous to the situation in Chapter 2, where using a suitable proof calculus avoided the problem of having to check infinitely many models of a set of predicate logic formulas in order to establish the validity of a sequent.

**Semi-automatic.** Although many of the steps involved in proving that a program satisfies its specification are mechanical, there are some steps that involve some intelligence and that cannot be carried out algorithmically by a computer. As we will see, there are often good heuristics to help the programmer complete these tasks. This contrasts with the situation of the last chapter, which was fully automatic.

**Property-oriented.** Just like in the previous chapter, we verify properties of a program rather than a full specification of its behaviour

**Application domain.** The domain of application in this chapter is sequential transformational programs. ‘Sequential’ means that we assume the program runs on a single processor and that there are no concurrency issues. ‘Transformational’ means that the program takes an input and, after some computation, is expected to terminate with an output. For example, methods of objects in Java are often programmed in this style. This contrasts with the previous chapter which focuses on reactive systems that are not intended to terminate and that react continually with their environment.

**Pre/post-development.** The techniques of this chapter should be used during the coding process for small fragments of program that perform an identifiable (and hence, specifiable) task and hence should be used during the development process in order to avoid functional bugs.

## 1.1 Why should we specify and verify code?

The task of specifying and verifying code is often perceived as an unwelcome addition to the programmer's job and a dispensable one. Arguments in favour of verification include the following:

**Documentation:** The specification of a program is an important component in its documentation and the process of documenting a program may raise or resolve important issues. The logical structure of the formal specification, written as a formula in a suitable logic, typically serves as a guiding principle in trying to write an implementation in which it holds.

**Time-to-market:** Debugging big systems during the testing phase is costly and time-consuming and local 'fixes' often introduce new bugs at other places. Experience has shown that verifying programs with respect to formal specifications can significantly cut down the duration of software development and maintenance by eliminating most errors in the planning phase and helping in the clarification of the roles and structural aspects of system components.

**Refactoring:** Properly specified and verified software is easier to reuse, since we have a clear specification of what it is meant to do.

**Certification audits:** Safety-critical computer systems – such as the control of cooling systems in nuclear power stations, or cockpits of modern aircrafts – demand that their software be specified and verified with as much rigour and formality as possible. Other programs may be commercially critical, such as accountancy software used by banks, and they should be delivered with a warranty: a guarantee for correct performance within proper use. The proof that a program meets its specifications is indeed such a warranty.

The degree to which the software industry accepts the benefits of proper verification of code depends on the perceived extra cost of producing it and the perceived benefits of having it. As verification technology improves, the costs are declining; and as the complexity of software and the extent to which society depends on it increase, the benefits are becoming more important. Thus, we can expect that the importance of verification to industry will continue to increase over the next decades. Microsoft's emergent technology A# combines program verification, testing, and model-checking techniques in an integrated in-house development environment. Currently, many companies struggle with a legacy of ancient code without proper documentation which has to be adapted to new hardware and network environments, as well as ever-changing requirements. Often, the original programmers who might still remember what certain pieces of code are for have moved, or died. Software systems now often have a longer life-expectancy than humans, which necessitates a durable, transparent and portable design and implementation process; the year-2000 problem was just one such example. Software verification provides some of this.