

Exercise 1

Two sources, each transmitting at 64 kbit/s, and another source transmitting at 640 kbit/s are multiplexed using Time Division Multiplexing (TDM).

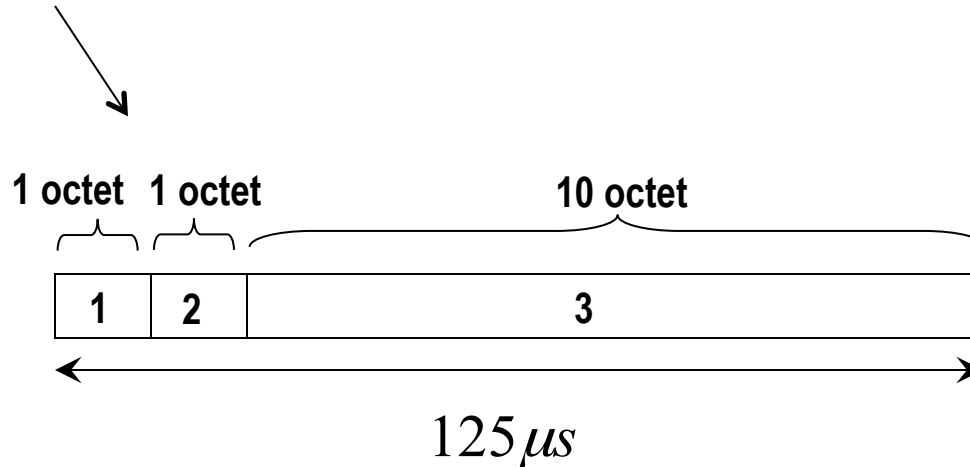
Let us assume that multiplexing is performed at the level of a single octet (byte, 8 bit). You need to find:

- 1) the *structure* of the frame having minimal duration
- 2) the *duration* of such frame
- 3) the *transmission rate* of the multiplexer (expressed in kbit/s)

Answer to the same questions above (1, 2 and 3) in the case where multiplexing is performed at the level of a single bit (1 bit).

Exercise 1 - Solution

Structure of the frame (3 time slots, each one for each source) :



$$\text{Frame duration} = \frac{8 \text{ bit}}{64 \text{ kbit} / s} = 125\mu s$$

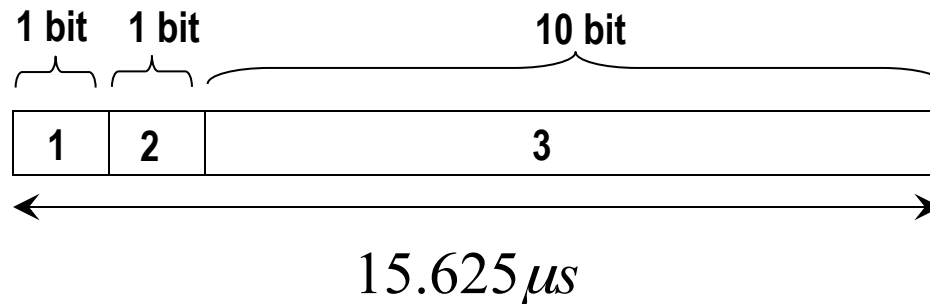
It's the time necessary for the slowest source (the one at 64 kbit/s) to accumulate the 8 bits necessary

$$\text{Transmission rate of the multiplexer} = \frac{12 \text{ byte}}{125 \mu s} = 768 \text{ kbit} / s$$

Exercise 1 - Solution

If multiplexing is performed at the level of a single bit (1 bit).

Frame structure :



$$\text{Frame duration} = \frac{1 \text{ bit}}{64 \text{ kbit} / s} = 15.625 \mu s$$

$$\text{Transmission rate of the multiplexer} = \frac{12 \text{ bit}}{15.625 \mu s} = 768 \text{ kbit} / s$$

Exercise 2

A multiplexing system based on TDM is characterized by a frame composed of 10 Time Slots; in each time slot, 128 bits are transmitted. The system is used to multiplex 10 telephone channels, each of which has a transmission rate of 64 kbit/s.

You need to determine the *transmission rate* of the multiplexer and the *duration* of the frame.

Exercise 2 - Solution

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Solution. The transmission rate of the multiplexer is 640 kbit/s (10×64 kbit/s) and the frame duration is $(128 \text{ bit} / 64 \text{ kbit/s}) = 2$ ms.

Alternatively: the frame duration is the time necessary for a telephone source to accumulate the 128 bits necessary: $128/64=2$ ms

Exercise 3

A cellular system utilizes a TDMA (Time Division Multiple Access) system for 100 telephone calls (100 channels), each of which transports voice encoded at 32 kbit/s. The cell radius is equal to 300 m, *timing advance* is not used, and we want the system to have an efficiency at least equal to 90%.

You need to determine:

- ◆ The *guard time* necessary in such system
- ◆ The size (expressed in bits) of the *TDMA burst* for each channel
(*burst* = number of bits transmitted for each source/telephone call inside the slot which is reserved to it)
- ◆ The frame duration (in seconds)
- ◆ The transmission rate of the TDMA multiplexer

The speed of propagation of the signal is equal to 300000 km/s.

Exercise 3 - Solution

The propagation time τ is equal to $\tau = 1 \mu\text{s}$, hence the guard time is equal to $2 \mu\text{s}$. The transmission burst must last at least for T , with $T/(T+2\tau)=0.9$, which gives $T=18\tau$. Therefore:

$$T = 18 \mu\text{s}.$$

The frame duration D , with $T=18\mu\text{s}$ is hence equal to $D=100*(18+2)=2000 \mu\text{s}$, hence $D=2 \text{ ms}$.

For each bit of each telephone call, the bits of each call/channel (the so called *burst*) are generated during the frame duration. Hence, the number of bits B of a burst is equal to $B=32000 \times 0,002=64 \text{ bits}$.

The B bits of each burst must be transmitted at a speed V (to be determined) such that $T= 18\mu\text{s}$ are used. Hence, the transmission rate of the TDMA multiplexer is equal to $V=64/18=3.555 \text{ Mb/s}$